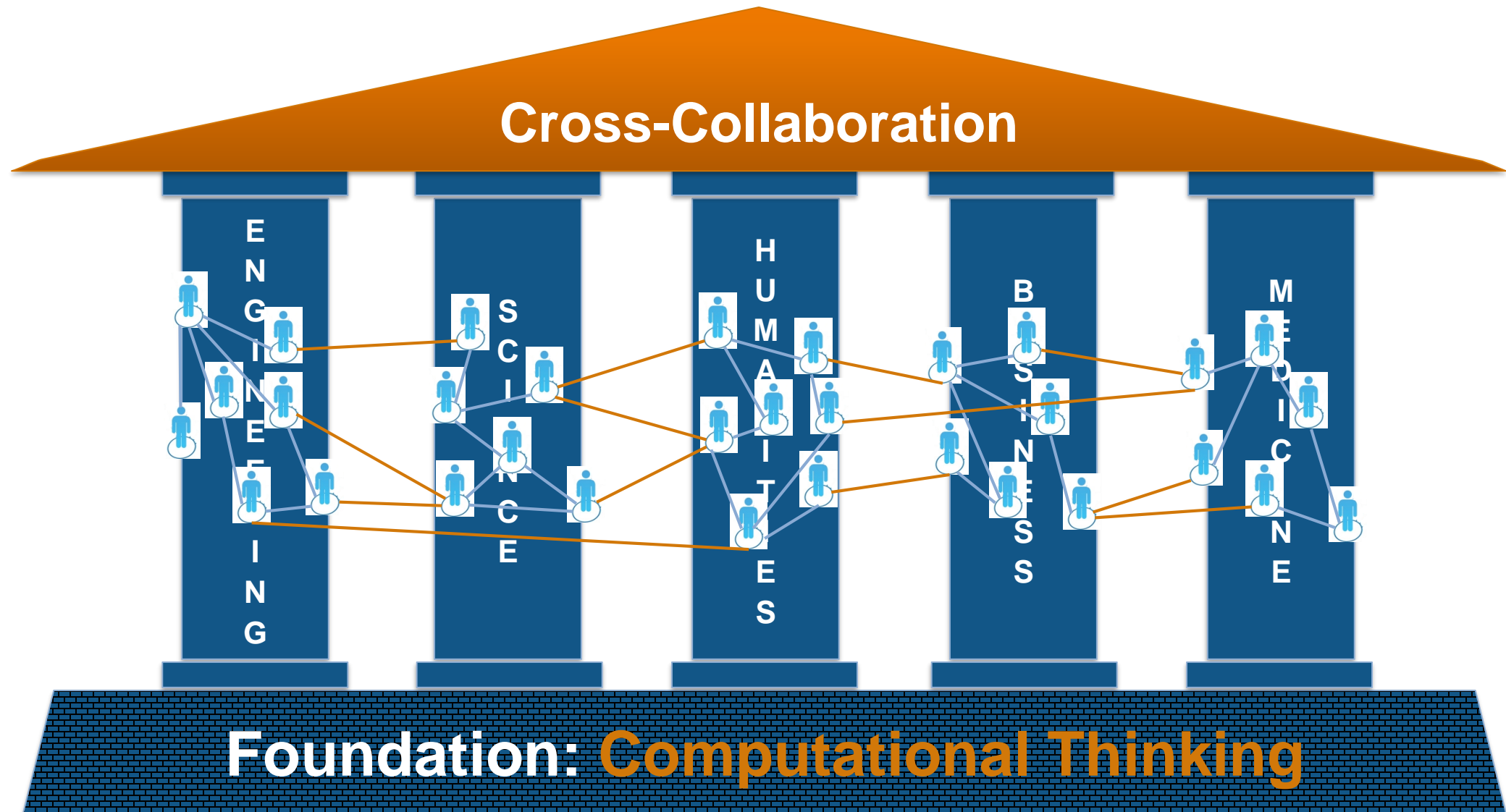


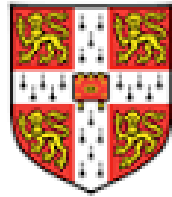
# Building Computational Thinking at Top Universities

**MathWorks**



# What Is Happening Elsewhere

**MOOC**



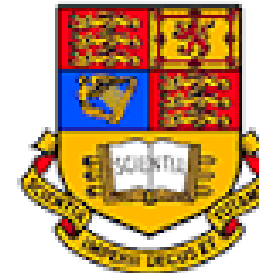
UNIVERSITY OF  
CAMBRIDGE

**Inverted classroom**



**Integrated  
curriculum**

**Computation**



Imperial College  
London

**Collaboration**

**Visualization**

**On-line learning**

# Computational Thinking

**A Thought Process to Formulate  
Problems and Solutions**



# Where Computational Thinking Fits

**Computational Thinking**

**Reading**

**Writing**

**Arithmetic**

# Computational Thinking is Important

Learn to Code



Code to Learn!

*"Computational thinking is a fundamental skill for everyone, not just for computer scientists."*

*Dr. Jeannette Wing, Vice President of Microsoft Research  
Former Department Head of CS at Carnegie Mellon University*

*"Coding teaches me to think in a logical way"*

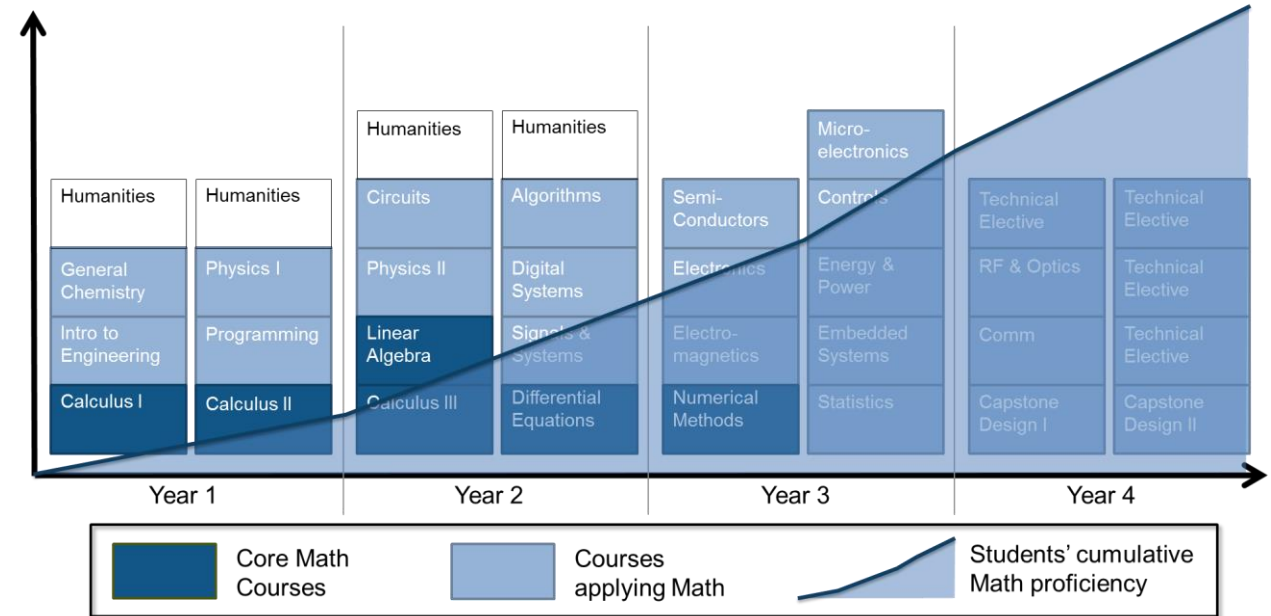
*Trinity School high school student*

*Accepted at MIT*

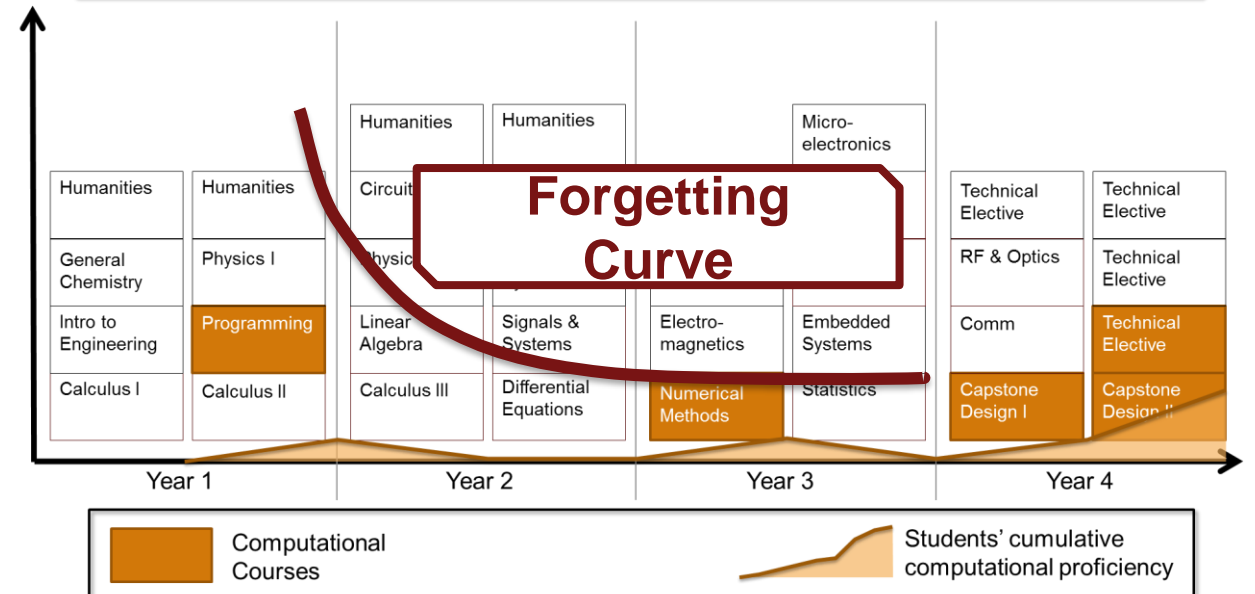


# Traditional Approach to Teaching

How Math is introduced in the curriculum



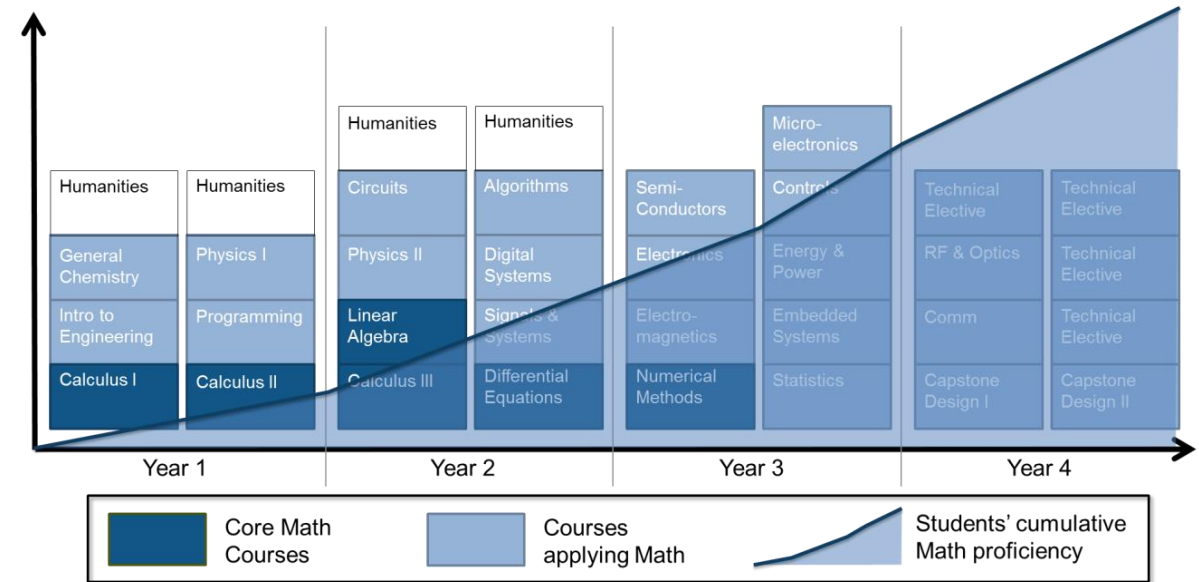
How Computational Thinking is introduced



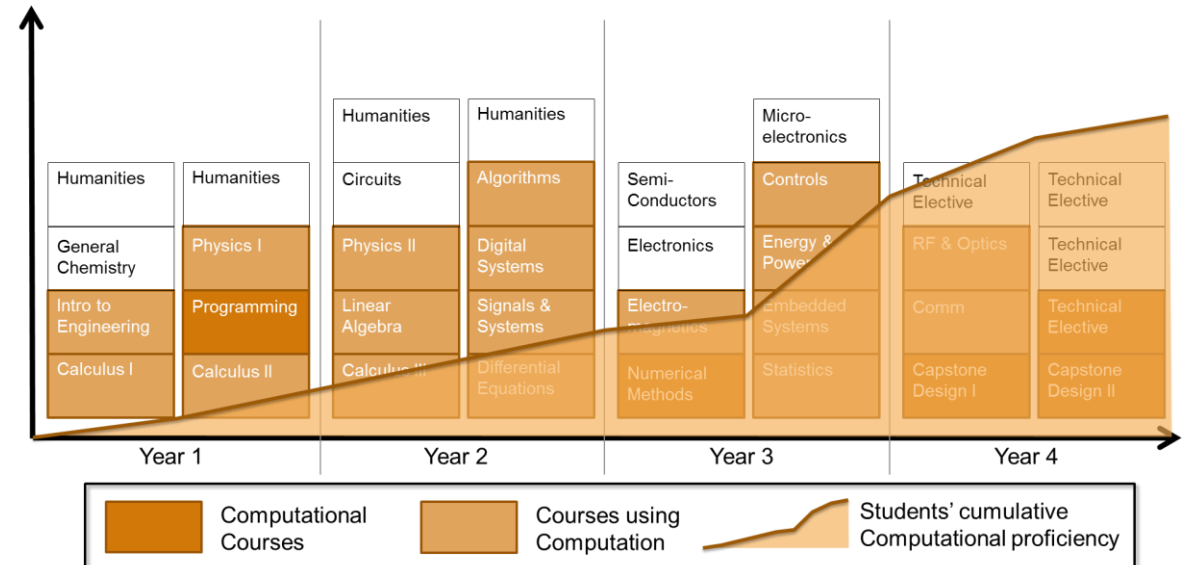


# The Future of How Computational Thinking Will be Taught

How Math is introduced in the curriculum



How Computational Thinking could be taught

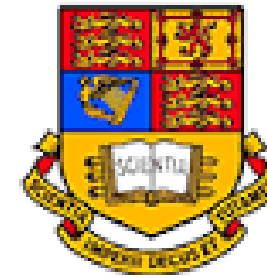




# How Top Universities Build Computational Thinking with MATLAB

## 1. Supplementing pen and paper

Imperial College



Imperial College  
London

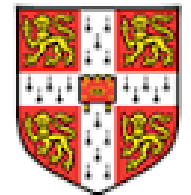
## 2. Using on-line learning

MIT



## 3. Integrating usage across classrooms

MIT & University of Cambridge



UNIVERSITY OF  
CAMBRIDGE

# **1. Supplementing pen and paper**

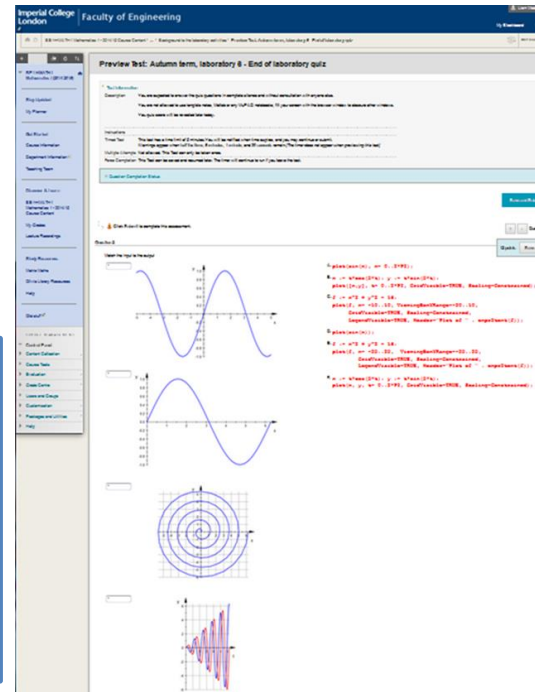
## **Visualization**

# The Mathematics Laboratory Imperial College London, Bioengineering

1. Lecture (YouTube / live)
2. Pen and paper study group
3. MATLAB laboratory
4. Formal assessment

## MATLAB to complement Mathematics teaching

- Brings Mathematics to life
- Engagement of brighter students
- Reinforcement learning



Autumn term:	
<ul style="list-style-type: none"> <li>Overview</li> <li>MuPAD quick reference</li> <li>An introduction to the MuPAD based laboratories <a href="#">video</a></li> <li>An introduction to Symbolic Algebra using MuPAD <a href="#">video</a></li> </ul>	
Alpha	Beta
Variables and functions: (heads-up: <a href="#">notebook/video</a> )	Curve sketching: (heads-up: <a href="#">notebook/video</a> )
Limits: (heads-up: <a href="#">notebook/video</a> )	Complex Numbers: (heads-up: <a href="#">notebook/video</a> )
Differentiation: (heads-up: <a href="#">notebook/video</a> )	Integration: (heads-up 1/2: <a href="#">notebook/video</a> ) (heads-up 2/2: <a href="#">notebook/video</a> )
Vector Algebra: (heads-up: <a href="#">notebook/video</a> )	
Mock Mastery Q&A and <a href="#">Formula sheet</a>	Mock Mastery Q&A
Spring term:	
<ul style="list-style-type: none"> <li>Overview</li> <li>Matlab quick reference</li> </ul>	
Gamma	Delta
Matrix Algebra	Differential Equations (heads-up: <a href="#">notebook/video</a> )
Plotting graphs from data	
Matlab programming	Series (heads-up: <a href="#">notebook/video</a> )
Matlab coursework and associated files <a href="#">courseworkFiles.zip</a>	
Mock Mastery Q&A	Mock Mastery Q&A

# From Symbolic to Multi-Paradigm Solutions

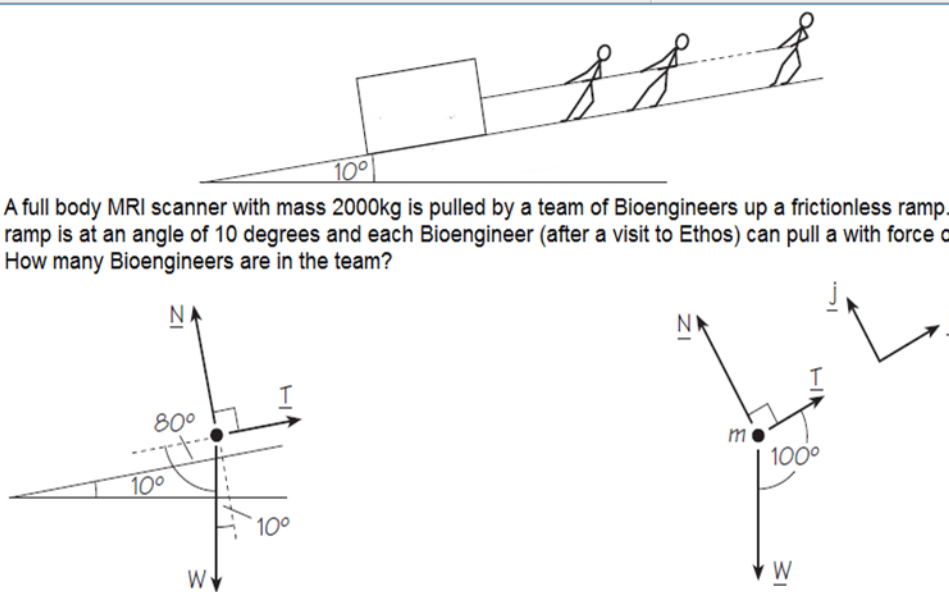
- Start with Symbolic Math
- Reinforce hand-calculations
- Move to multi-paradigm solutions for real engineering problems

```
>> g = 10, mass = 2000
g =
    10
mass =
    2000
>> m = [cos(degtorad(10)),
        cos(degtorad(100)),
        sin(degtorad(10)),
        sin(degtorad(100))]
m =
    0.9848    -0.1736
    0.1736     0.9848
>> inv(m) * [0 ; mass*g]
ans =
    1.0e+04 *
    0.3473
    1.9696
>> ans(1) / 315
ans =
    11.0253
```

Notebook1\* - MuPAD

File Edit View Navigation Insert Format Notebook Window Help

Generic Monospace 11



A full body MRI scanner with mass 2000kg is pulled by a team of Bioengineers up a frictionless ramp. The ramp is at an angle of 10 degrees and each Bioengineer (after a visit to Ethos) can pull a with force of 315N. How many Bioengineers are in the team?

```
reset(); DIGITS := 4: g := 10: deg2rad := PI/180: mass := 2000:
W := matrix([mass*g*cos(-100*deg2rad), mass*g*sin(-100*deg2rad)]);
T := matrix([[t, 0]]): N := matrix([[0, n]]):
solve(W + N + T = 0, [n,t]); float(%);
( -20000 cos(4π/9) -20000 sin(4π/9) )
{ [ n = 20000 sin(4π/9), t = 20000 cos(4π/9) ] }
{ [ n = 19700.0, t = 3473.0 ] }
pullForce := 315; float(3473/pullForce);
315
11.03
```

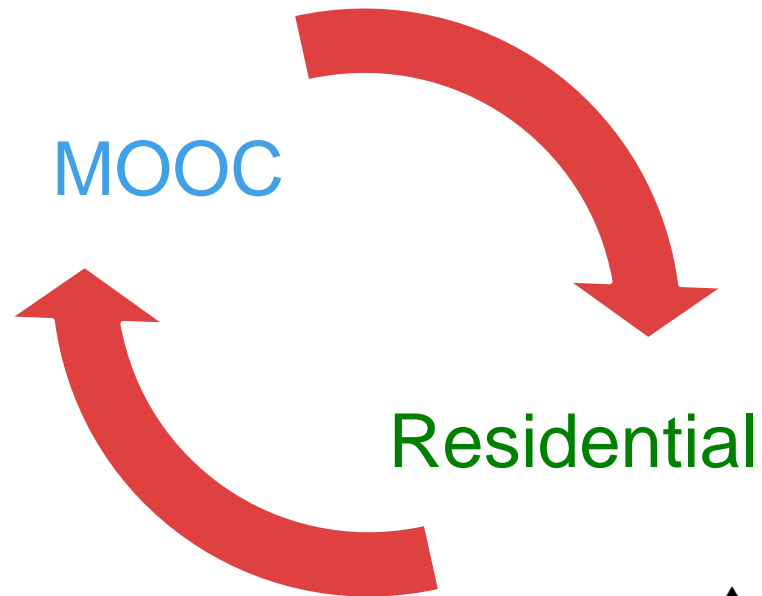
## **2. Using on-line learning**

**On-line course**

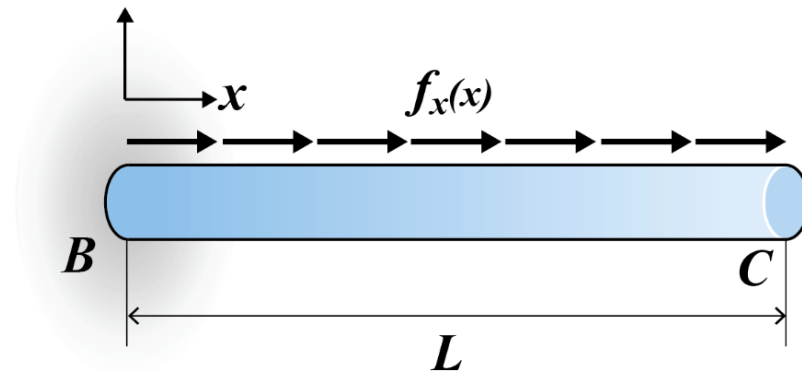
# MIT Mechanical Engineering

## 2.01x Elements of Structures, Required for 2<sup>nd</sup> year students

Simona Socrate



- Was a paper and pencil class
- Moved the material to edX as a MOOC
- Material is evolving through a constant cycle of residential classes and public MOOC offerings



# Different style of learning: Written Lecture Notes

## Axisymmetric Shafts in Torsion

### Loading Conditions on each Section (x)

Applied loading only around the axis ( $x$ ) of the shaft.

The only internal resultant at any sections  $\perp x$  is the axial torque  $T(x)$



**Find**  $T(x)$  along the bar (**axial torque diagram**) by cutting the bar at  $x$  and imposing moment equilibrium.

For the example shown, equilibrium at  $x$  gives:

$$\text{for } x < x^B : \sum M_x = 0 = -T(x) + Q^C + Q^B \rightarrow T(x) = Q^C + Q^B$$

$$\text{for } x > x^B : \sum M_x = 0 = -T(x) + Q^C \rightarrow T(x) = Q^C$$

And the entire axial torque diagram is:

For distributed loading  $t(x)$ , with  $t(x)$  [in (N\*m)/m = N]  $\oplus$  with right hand rule along  $x$ , obtain the torque  $T(x)$  by integrating  $t(x)$  along the shaft. For the shaft shown:

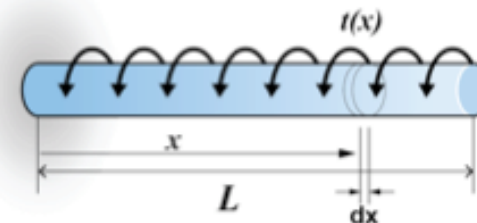
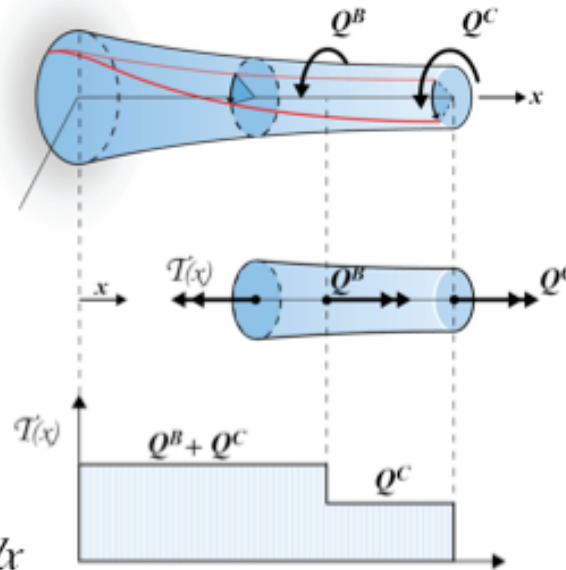
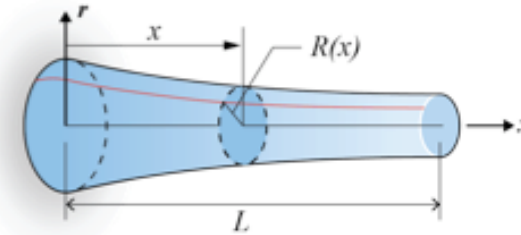
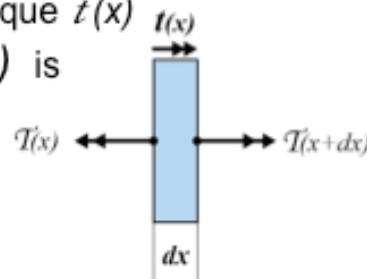
$$T(x) = \int_x^L t(x) dx$$

The differential relationship

between the distributed torque  $t(x)$

and the axial resultant  $T(x)$  is

$$\frac{dT(x)}{dx} = -t(x)$$





## Different style of learning: Short Video Lectures



shafts in Torsion

Axial Loading  
Cross section displaces by  $u$

Slot

$$\epsilon_a = \frac{du_x}{dx} = \epsilon_a(x)$$

11:14 / 20:49

# Concept Questions in reading and video

E6\_2\_1

(1 point possible)

Obtain a symbolic expression for the effective section stiffness of the shaft,  $(GI_p)_{Eff}$ , in terms of  $R_0$  and  $G_0$

(enter this)

E6 2 | Torsion of Axisymmetric Shafts | 2.01x  
Courseware | edX

?

$(GI_p)_{Eff} =$

CHECK

E6\_2\_2

(1 point possible)

Obtain a symbolic expression for the  $x$ -rotation field along the shaft,  $\varphi(x)$ , in terms of  $R_0$ ,  $G_0$ ,  $L$ ,  $Q$ , and  $x$ .

(Note the direction of  $x$  in the figure):

?

$\varphi(x) =$

CHECK

# Online recitations

VR7\_1a

R7\_1A: REFINED

In this video, we will find the maximum value of the bending moment  $M(x)$  for the beam shown.

R7\_1A: REFINED  
(4 points)

$$M(x) =$$

$$M(x) =$$

$$M_{\max}^+ =$$

Start of transcript. Skip to the end.

PROFESSOR: Hi everyone, and welcome back to 2.01x recitation.

In this segment, we're going to do a number of examples of finding the moment diagram for beams under various loading conditions.

So let's get started with a simple one.

So we're just going to have our beam supported by two pins.

So we've got something like this.

CHECK

Download video

Download transcript

.srt ▾

# MATLAB Problem Sets

E6\_1: SHEAR STRAIN AND SHEAR STRESS IN A COMPOSITE SHAFT

E6\_1\_2

E6\_1\_4X

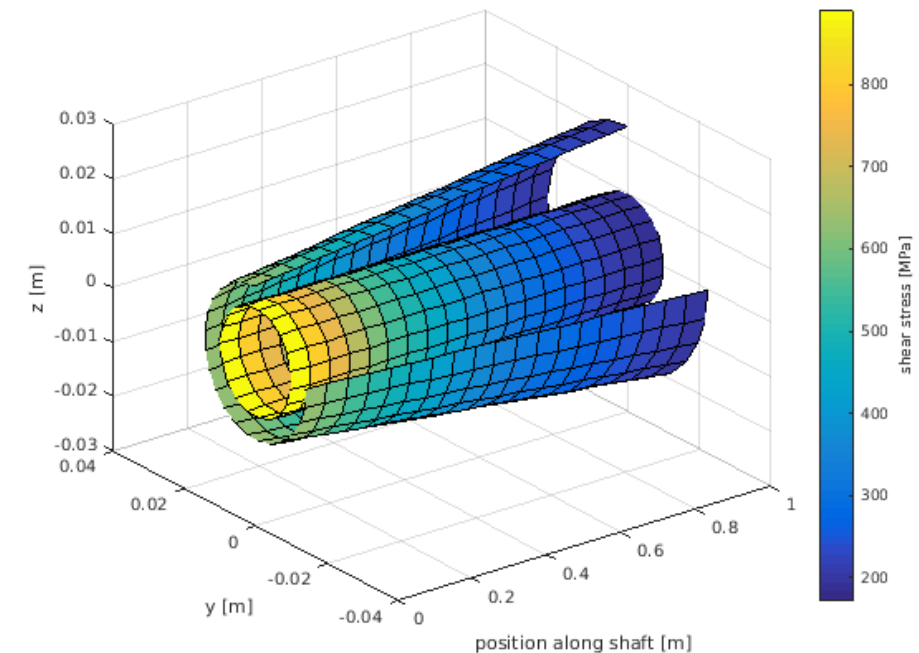
(1/1 point)

Use the MATLAB window below to verify your solution to part (4) above: obtain the values of the maximum shear stress in the sleeve  $\tau_{s,\max}$  and in the core  $\tau_{c,\max}$  on each section  $x$ , for  $0 \leq x \leq L$ . For  $\tau_{s,\max}$  and  $\tau_{c,\max}$  make sure you have the numeric values in MPa, and use corresponding MATLAB variables `tau_c_max` and `tau_s_max` in your script. EXTRA STEP: Try to obtain a plot with both curves,  $\tau_{s,\max}$  and  $\tau_{c,\max}$  as a function of position  $x$  along the shaft (the plotting task is not checked). Do the two curves cross at your predicted value  $x^*$ ?

```
1 % Create variables representing the given quantities
2 L = 1;           % in [m]
3 R0 = 0.01;       % in [m]
4 G0 = 70E9;       % in [Pa]
5 G0 = 70E9;       % in [Pa]
6 T = 3500;        % in [N·m]
7 x=linspace(0,L,20); % a vector of (20) x positions along the shaft
8
9 % Your code below
10 % re-use the same script of part 2x.....
11
12 RA = sqrt(2)*R0; %outer radius at A
13 RB = sqrt(5)*R0; %outer radius at B
14 R=RA+(RB-RA)*x/L; % a vector with outer radius of the shaft at each x position
15 Gc=2*G0;         % shear modulus of the core
16 Gs=G0;           % shear modulus of the sleeve
```

Correct

Figure 1



CHECK

RESET

SHOW ANSWER

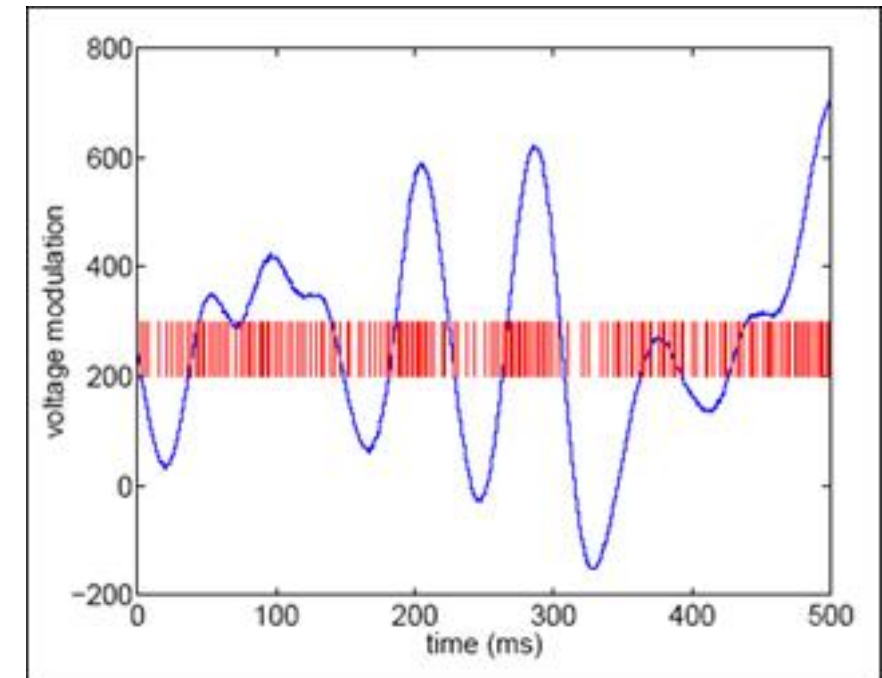
NOTE: this is probably the MOST challenging problem you have seen so far. I strongly suggest you do the three recitation problems before you try this one. The MATLAB scripts are quite long, and use tricks you might not have seen before, but they are quite nifty and you might like them! Try doing as much work as you can before you reveal the solutions, and try playing with the MATLAB answer scripts to understand how they work.

# **3. Integrating usage across classrooms**

**Integrated curriculum**

# MIT – Department of Brain and Cognitive Sciences

- Request from industry and graduate research
  - None of undergraduate courses taught computation
  - Moved to **introduce quantitative material earlier**
- Hired instructor for a transition to more computation (MATLAB) in courses
  - 9.40 Introduction to Neural Computation (required UG)
  - 9.54 Computational Aspects of Biological Learning (elective UG)
  - 9.011 Systems Neuroscience (required G – level setting incoming student knowledge)
- MATLAB Bootcamp, office hours

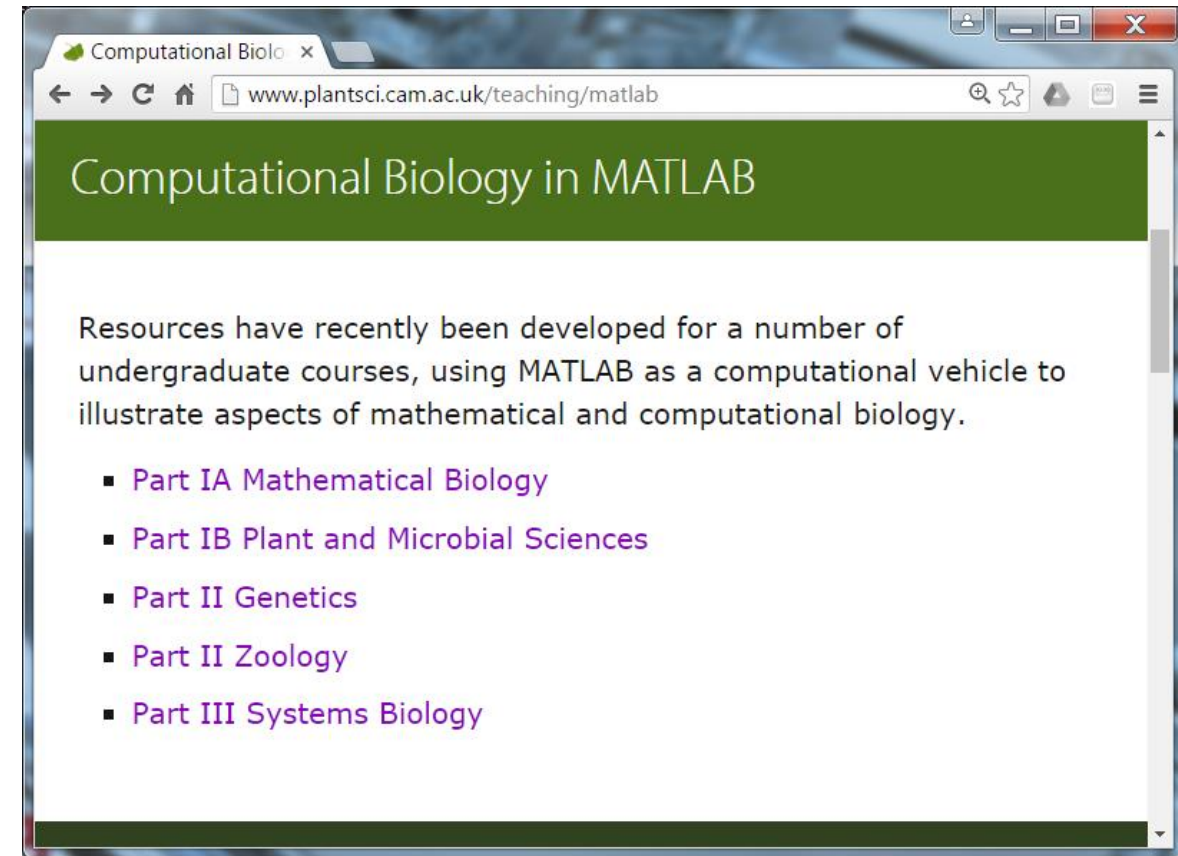


Taken from: MIT OCW 9.29



# University of Cambridge Biological Sciences

- Natural Science Course at Cambridge Biological Sciences stream
  - MATLAB Course complement Math (Year 1)
  - Reinforcement & math modelling in Plant & Microbial Science (Year 2)
  - Genetics and Zoology using the modelling skills (Year 3)
  - Systems Biology – Modelling techniques (Year 4 or Masters)





# Laboratory Exercises

- Word problems
- Apps
- Scripts & functions
- Visualizations

## Task 4

Suppose instead the patient is able to take an oral pain killer. A tablet containing 30mg of the same pain-relief agent is administered. The absorption rate of the drug from the gut into the blood plasma  $b = 0.24$  per hour and the elimination rate of the drug  $k = 0.28$  per hour.

- Draw a schematic diagram to illustrate the new system and write down the governing equations and fluxes.
- Solve the equation for the absorption compartment and insert the solution into the central compartment. You should get:

$$V_2 \frac{dC_2}{dt} = bV_1 C_0 e^{-bt} - kV_2 C_2 = bDe^{-bt} - kV_2 C_2$$

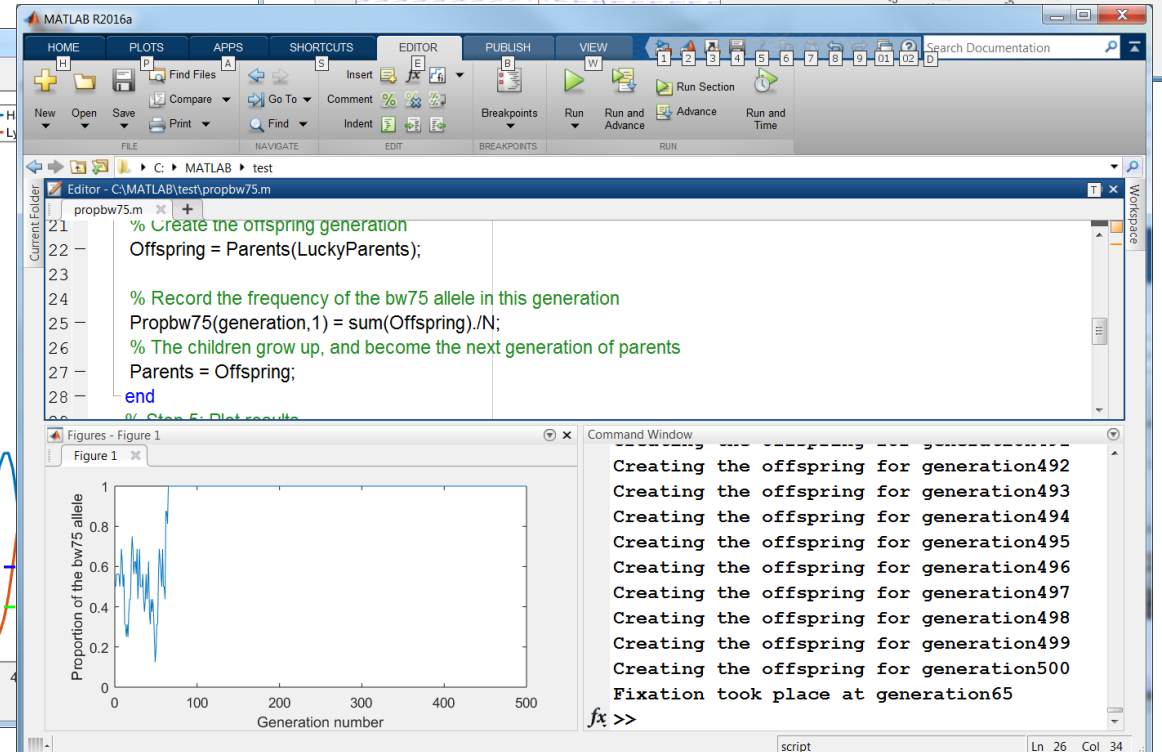
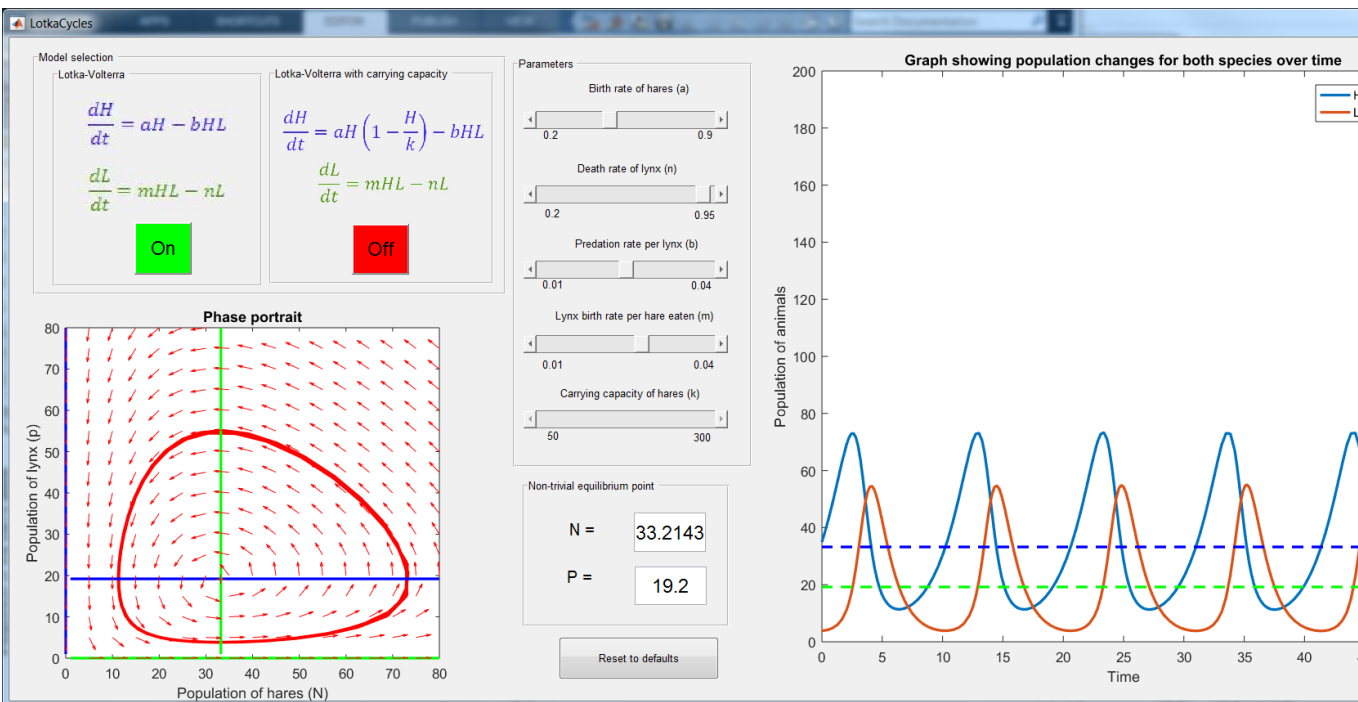
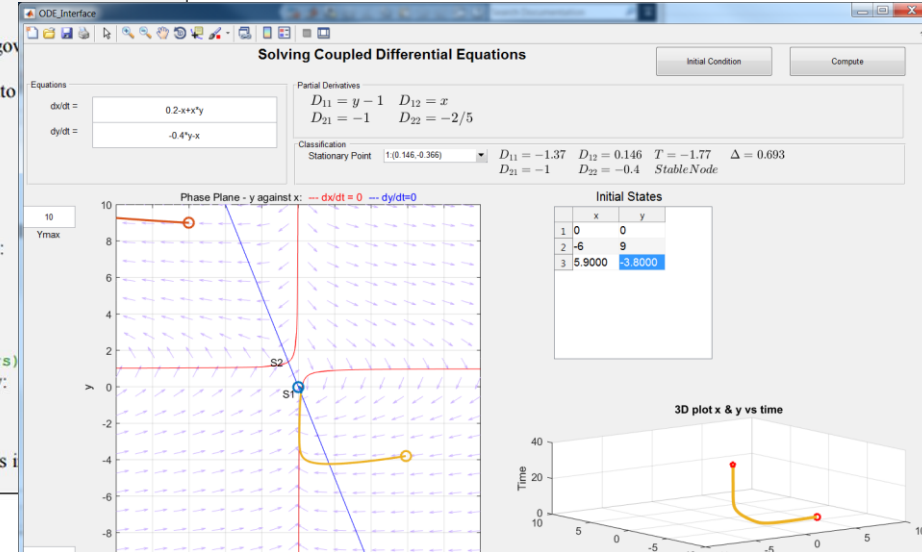
Where  $D$  is the dose of drug.  $V_2 = V_d = 210$  litres.

- Modify your script code to solve this model

**Hints:** (i) make sure you have adjusted component 2 of your code correctly:

```
Vd = 210; % volume of distribution litres
Dose = 25*1000; % milligrams* 1000 gives micrograms
Cinit = 0; % no drug in body at time 0 as oral dose
b = 0.15; % per hour
k = 0.28; % per hour
tmax = 12; % time range over which to solve model (hours)
Ji = @(t,C) b.*Dose.*exp(-b.*t); % influx
Je = @(t,C) k.*C.*Vd; % efflux
```

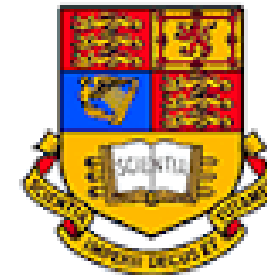
- How long does it take blood plasma concentration to reach therapeutic levels



# How Top Universities Build Computational Thinking with MATLAB

## 1. Supplementing pen and paper

Imperial College



Imperial College  
London

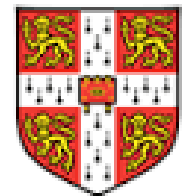
## 2. Using on-line learning

MIT



## 3. Integrating usage across classrooms

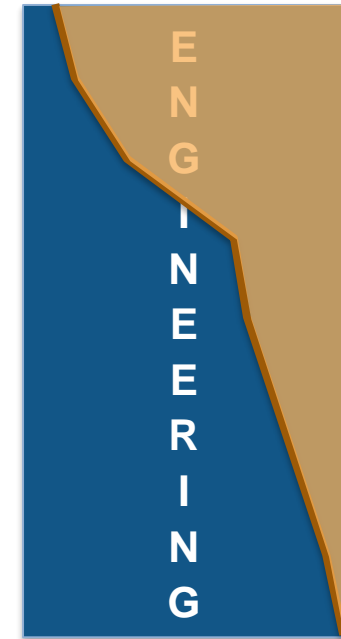
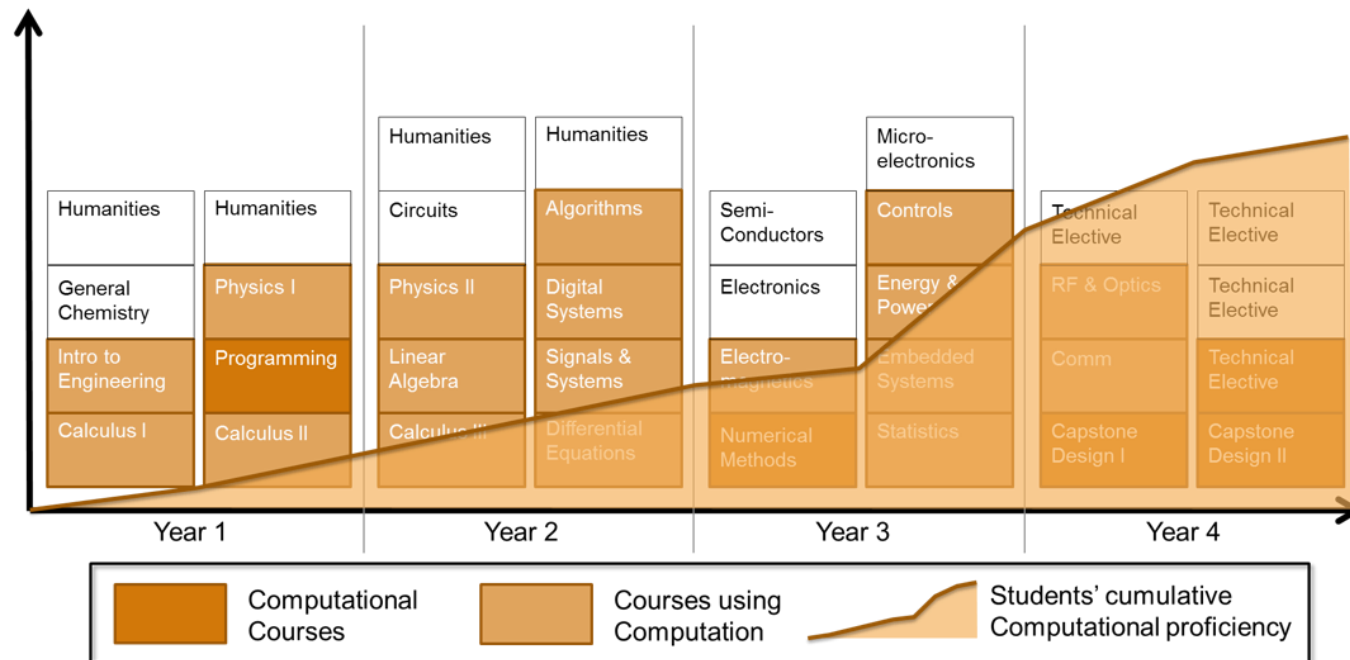
MIT & University of Cambridge



UNIVERSITY OF  
CAMBRIDGE

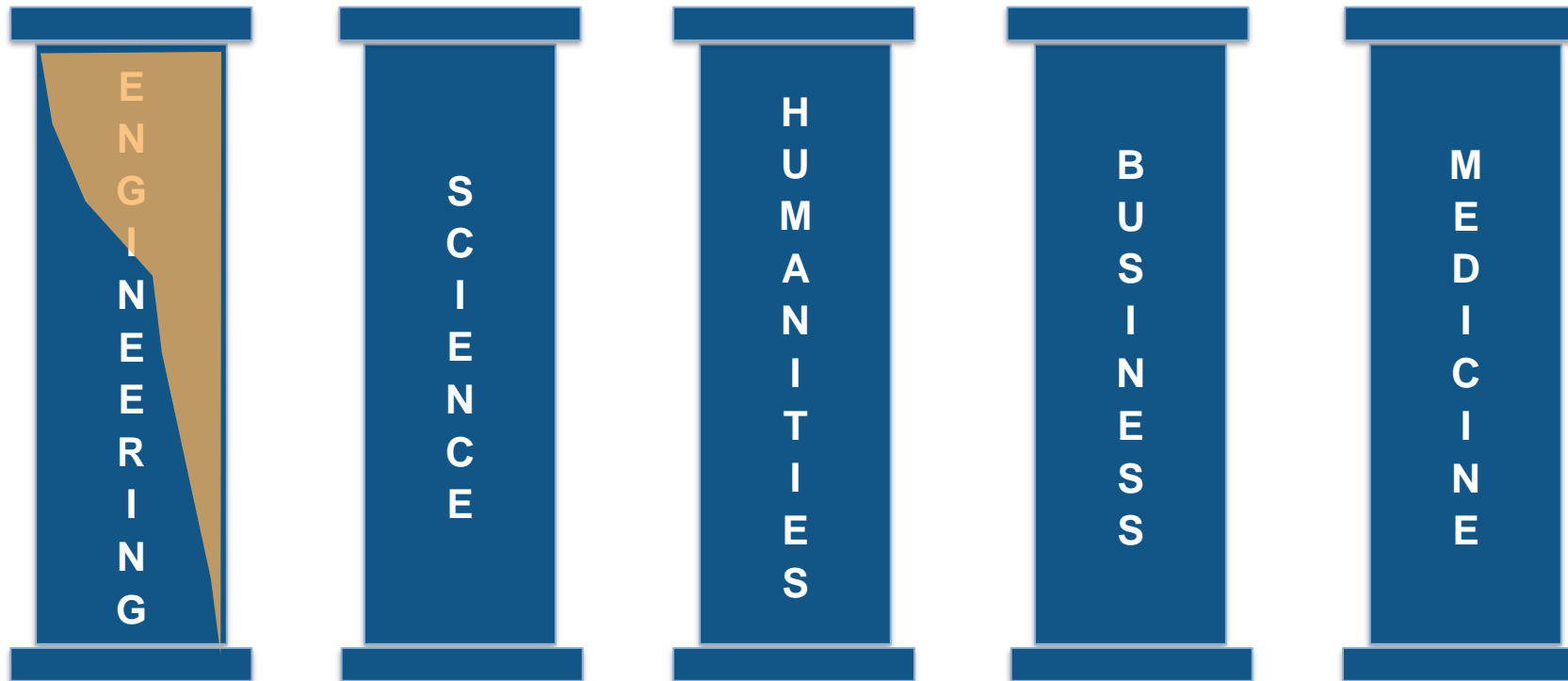
# Integrated Curriculum Builds **Depth** within the Domain

## What about **Breadth**?



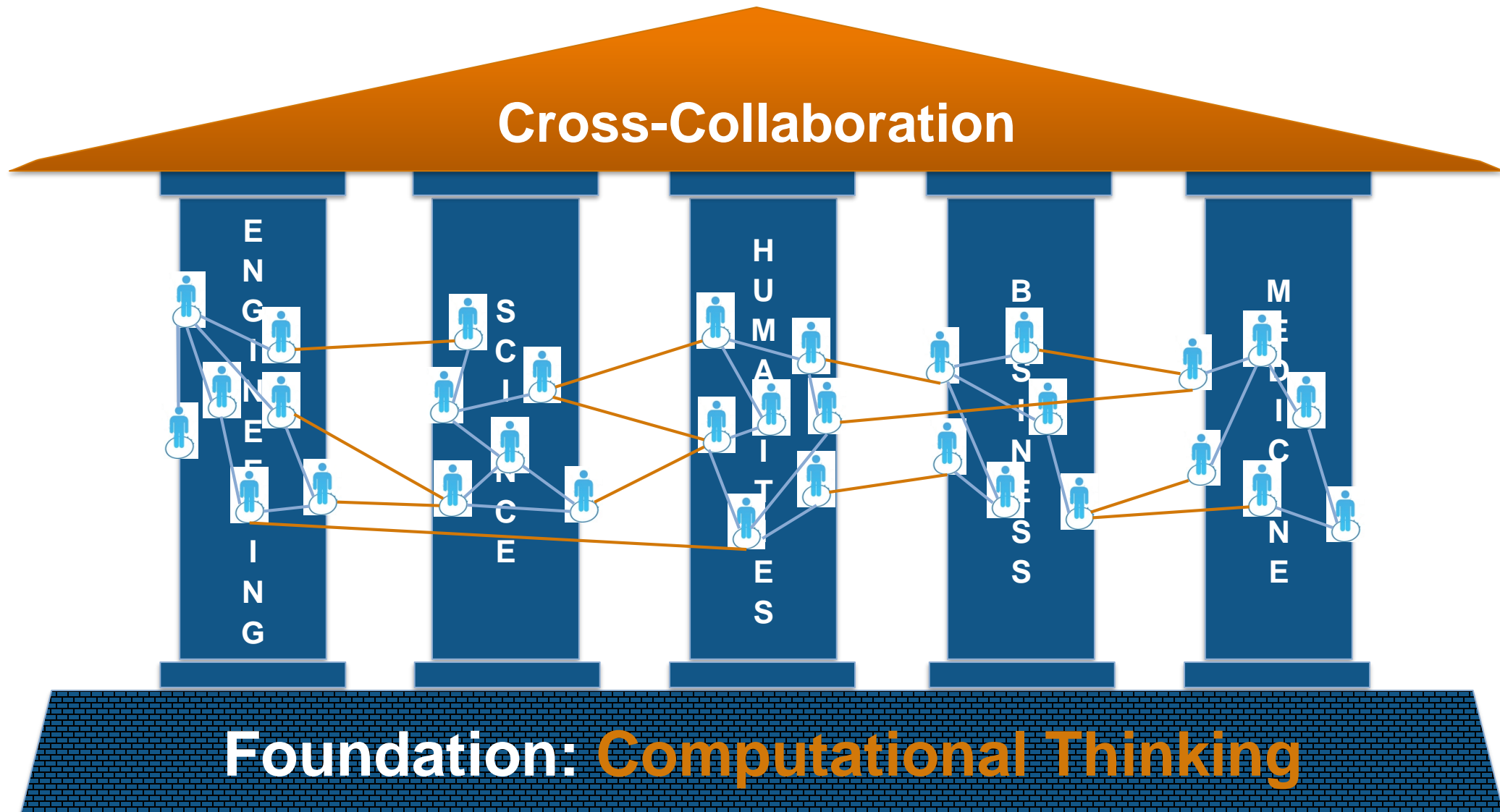
# Is This Just About Engineering?

**Schools and Colleges are Siloed by Nature**



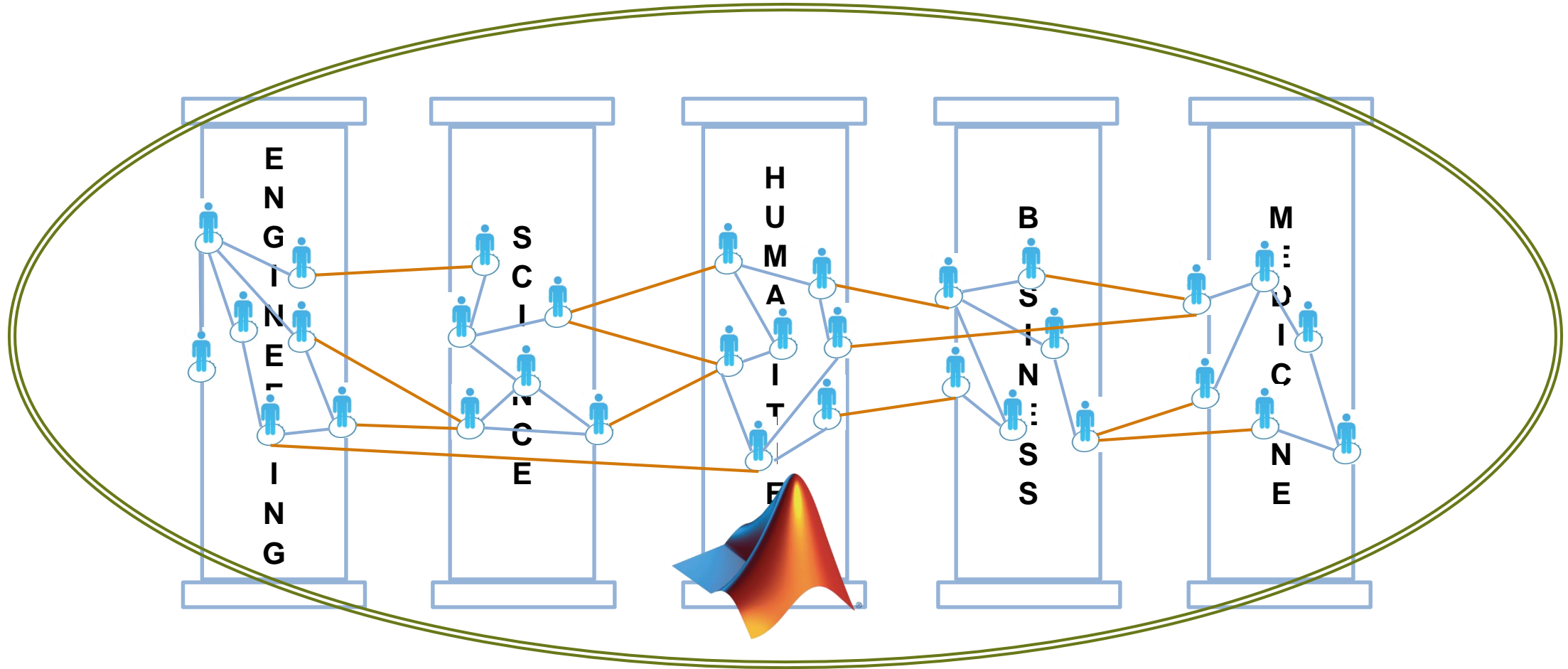
**Real World Problems Are Multidisciplinary  
and Require Collaboration across Domains**

# What if Computational Thinking Was Commonplace?



# Computational Thinking – One Common Language

Integrated Curriculum → Integrated Campus



**MATLAB Enabled Campus for Everyone, Anywhere**